

Proportional Reasoning

Ratios and proportions are used often in mixtures to keep a balance between ingredients.

Ex 1

An equivalent ratio can be made by multiplying or dividing all components by a constant amount.

Write an equivalent ratio for each given ratio

a) $3 : 6 = \underline{12} : \underline{24}$ b) $4 : 9 = \underline{8} : \underline{18}$

Handwritten notes: "x4" with an arrow pointing from 3 to 12 and from 6 to 24. "ratio" written below the first equation.

c) 6 to 10 = $\underline{3}$ to $\underline{5}$

Handwritten note: "÷2" with an arrow pointing from 6 to 3 and from 10 to 5.

Ex 2 proportion statement

A proportion is a statement to say that two ratios are equal. They can be used to solve mixture problems.

Orange Juice is made by combining 3 parts of water with 1 part of concentrate. If 9 parts of water are used to make Orange Juice then how much concentrate must be used?

Water: concentrate
 $3 : 1 = 9 : C$

$$\frac{3}{9} = \frac{1}{C}$$

$$\frac{3C}{3} = \frac{9}{3}$$

$C = 3$ part concentrate

Ex 3

More complicated problems can incorporate more than two elements in the mixture.

A recipe for math biscuits uses 5 cups of flour, 1 cup of sugar and 2 cups of milk. How much flour and sugar must be used to make the biscuits if we have 4 cups of milk?

Flour: Sugar: Milk
 $5 : 1 : 2 = F : G : 4$

$$\frac{5}{F} = \frac{1}{G} = \frac{2}{4}$$

$$\frac{5}{F} = \frac{2}{4}$$

$$\frac{2F}{2} = \frac{20}{2}$$

F = 10 cups
of flour

$$\frac{1}{G} = \frac{2}{4}$$

$$\frac{2G}{2} = \frac{4}{2}$$

G = 2 cups
of sugar